A method to estimate the number of neurons supporting visual orientation discrimination in primates [version 1; referees: 2 approved]

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Abstract
In this method article, we show how to estimate the number of retinal ganglion cells (RGC), and the number of lateral geniculate nucleus (LGN) and primary visual cortex (V1) neurons involved in visual orientation discrimination tasks. We reported the results of this calculation in Kanitscheider \textit{et al.} (2015), where we were interested in comparing the number of neurons in the visual periphery versus visual cortex for a specific experiment. This calculation allows estimation of the information content at different stages of the visual pathway, which can be used to assess the efficiency of the computations performed. As these numbers are generally not readily available but may be useful to other researchers, we explain here in detail how we obtained them. The calculation is straightforward, and simply requires combining anatomical and physiological information about the macaque visual pathway. Similar information could be used to repeat the calculation for other species or modalities.

Keywords
visual cortex, vision, population coding

This article is included in the INCF gateway.
Introduction
We would like to estimate:
1) the number of RGC and LGN neurons activated by a given visual stimulus; and
2) the number of V1 neurons that are activated by the same stimulus and are relevant to compute orientation.

We define as relevant those neurons that project to higher cortex, and separately consider the additional requirement that the neurons are tuned for orientation.

Methods
Upper bound on the number of cortical neurons
First, the number of neurons activated by a visual stimulus depends on the size and position of the image in the visual field. We use as a reference the setup of Dosher & Lu (1998) in experiments with human subjects, but the calculation reported below can be readily applied to visual stimuli of different size and position. Stimuli are presented parafoveally, at eccentricities between 2 and 5 degrees, and cover an area of 1x1 to 2x2 deg^2 in the visual field. To illustrate the calculation, we assume a 1x1 deg^2 stimulus at an eccentricity of 3 degrees.

The second factor is the volume of the cortex (surface x depth) that is activated by such stimuli. To estimate the surface we use cortical magnification factors (number of neurons per deg^2, as a function of eccentricity). We use here the results of Van Essen et al. (1984) who found that the following equation captured the relation between eccentricity (E, in degrees) and cortical surface activated by a 1x1 deg^2 stimulus (M, in mm^2/deg^2):

\[ M = 103(0.82 + E)^{-2.28} \]  
(1.1)

Hence, presenting a 1x1 deg^2 stimulus at an eccentricity of 3 degrees should activate a cortical surface of approximately 5 mm^2.

To determine cortical depth, we assume that the only V1 neurons used to solve a visual task are those that project to higher cortex, i.e. pyramidal neurons in layers 2/3/4B (Peters & Rockland, 1994, ch. 1), and approximately 80% of neurons in V1 are excitatory (Peters & Rockland, 1994, ch. 1), hence we consider an effective depth of 0.8x0.75=0.6 mm. Combining this with the estimated surface of 5 mm^2, we obtain an effective volume of 3 mm^3.

We then multiply this volume by cortical density, which in V1 is approximately 120,000 neurons/mm^3 (O’Kusky & Colonnier, 1982). This leads to an estimate of 360,000 neurons/deg^2. This number represents an upper bound, assuming that all neurons contribute to decoding orientation regardless of their individual tuning for orientation. This is a reasonable assumption as long as the variability of untuned neurons is correlated with that of tuned neurons (Zylberberg, 2017) or the tuning is not perfectly flat.

Lower bound on the number of cortical neurons
To obtain also a lower bound, we consider the alternative that only neurons selective for orientation are relevant for orientation discrimination. Ringach et al. (2002) characterized the distribution of orientation selectivity in V1 across layers. Using bandwidth (half of the tuning curve width at 1/2 height) as a measure of selectivity, if we include only neurons with bandwidth smaller than 30 degrees we find that, across layers 2/3/4B, approximately 75% of the neurons satisfy the criterion. The threshold of 30 degrees is arbitrary; we chose a rather small threshold to obtain a lower bound. Combining the above estimates, the lower bound on the number of V1 neurons that can be used by downstream areas for orientation discrimination in the experimental setting considered here is 270,000. This is the estimate reported in Kanitscheider et al. (2015).

An additional consideration is that typical extracellular recordings with single electrodes, as in Ringach et al. (2002), tend to be biased towards neurons that are visually responsive (i.e. activity evoked by their preferred stimulus is substantially larger than spontaneous activity) and have high firing rates (Olshausen & Field, 2005), raising the possibility that we overestimated the proportion of tuned neurons. Data recorded with chronically implanted multielectrode arrays (Kelly et al., 2007), which do not suffer from these biases, indicate that the proportion of tuned neurons in L2/3 is consistent with Ringach et al. (2002). However, if some neurons were entirely silent throughout a recording session, i.e. they did not fire even a spontaneous action potential, they would go undetected, thus positively biasing the proportion of tuned neurons. We are not aware of direct estimates of the number of such neurons in macaque, but we can use as a guidance recent studies of rodent V1. Using calcium imaging, Ko et al. (2014) found that 55% of all neurons in a small volume are responsive to at least one visual stimulus, indicating that silent neurons represent at most 45% of the population. If we further assume that silent neurons do not contribute to orientation discrimination, we are left with a proportion of 0.75x0.55, or approximately 150,000 neurons. This represents a loose lower bound.

Estimating the number of LGN and retinal neurons
The LGN volume and number of neurons activated by the same visual stimulus can be computed similarly from cell magnification factors derived by Malpeli et al. (1996) for parvocellular and magnocellular layers, respectively:

\[ N_p = 1.011,688(2.9144 + E)^{-1.6798} \]
\[ N_m = 2.620.2(5.5638 + (E−1.8322))^−0.8012 \]  
(1.2)

The above leads to an estimate of approximately 9,000 LGN neurons for a 1x1 deg^2 stimulus at an eccentricity of 3 degrees.

Lastly, to estimate the number of RGCs we used the cell magnification factors provided by Malpeli et al. (1996) figure 11 (based on Wässle et al., 1990), who assumed a constant
fraction of RGCs projecting to LGN (90%) and binocular viewing conditions. We then interpolated linearly between the reported RGC densities at eccentricities of 5 degrees (3,000 cells/deg²) and 2 degrees (8,500 cells/deg²), and obtained an estimate of approximately 6,500 RGCs for a 1×1 deg² stimulus at an eccentricity of 3 degrees.

Discussion
We have illustrated a method to estimate the number of neurons involved in a visual orientation discrimination task. The method involves considerations about experimental stimuli, including their size and position in the visual field, and considerations about the anatomy of the visual system, including magnification factors and neuron density. By considering different possible requirements for the subset of neurons that may be involved in the task, we have derived lower bounds on the estimates. Our results suggest an LGN-V1 expansion ratio between 17:1 and 40:1, similar to values reported previously for visual cortex (DiCarlo et al., 2012; Olshausen & Field, 2004), and other sensory pathways (Brecht & Sakmann, 2002; DeWeese et al., 2003; Mombaerts et al., 1996). Similarly, the RGC-V1 expansion ratio is between 23:1 and 55:1. The method could be readily applied to different stimuli and other visual areas.

Competing interests
No competing interests were disclosed.

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The Coen-Cagli et al. paper is useful, showing a reasonable way to use known physiology and anatomy to estimate the number of neurons responding to a stimulus. This may be useful towards the long term goal of figuring out how the brain puts together the activity of multiple neurons to make perceptual decisions.

Is the rationale for developing the new method (or application) clearly explained?
Yes

Is the description of the method technically sound?
Yes

Are sufficient details provided to allow replication of the method development and its use by others?
Yes

If any results are presented, are all the source data underlying the results available to ensure full reproducibility?
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Are the conclusions about the method and its performance adequately supported by the findings presented in the article?
Yes

Competing Interests: No competing interests were disclosed.

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The authors provide a concise summary of the figures that go into estimating the number of neurons in retina, LGN, and V1 that are involved in a visual discrimination task. There are clearly a number of assumptions that go into such a calculation, but the authors do a good job of stating these assumptions explicitly and citing the relevant literature. One exception is the figure that 90% of RGCs project to LGN (specifically dorsal LGN in this case). This figure will also depend on eccentricity because the proportion of parasol and midget RGCs (which do project to dLGN) depends on eccentricity. In peripheral retina, the fraction of dLGN-projecting RGCs is far below 90% in primates. With this relatively simple fix, I think this short paper will provide a nice reference for calculations of cell counts in the early visual pathways.

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Yes

Is the description of the method technically sound?  
Yes

Are sufficient details provided to allow replication of the method development and its use by others?  
Yes

If any results are presented, are all the source data underlying the results available to ensure full reproducibility?  
No source data required

Are the conclusions about the method and its performance adequately supported by the findings presented in the article?  
Yes

Competing Interests: No competing interests were disclosed.

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