Abstract
Multicellular life is based on the ability of cells to divide, differentiate, cooperate and die in a controlled and organised manner, generating and maintaining an organism. The temporal distribution of division, differentiation and death determines the cellular composition of the organism at any particular point in time. Like these ontogenetic events, phylogenetic development takes place with the changes in total cell numbers, the allocation of these cells to different tissues and the disappearance of certain tissues.
Fractal properties of complex networks, a result of growth, can be estimated by box counting, whereby the topological properties of the network are mapped by changing the resolution of examination, that is changing the size of the boxes used to identify and group network components. Here we develop the concept of cellular box-counting, referring to the fact that cells can be grouped on various levels of hierarchy and these various levels can be interpreted as boxes of different linear sizes. We apply the method to data representing distinct stages and groups of evolution of life and interpret the network properties of brown algae, green plants and animals. The results are in agreement with previously established values of degree exponent of biological networks and provide clues to the differences in the network organization of multicellular life.

Keywords
network, fractal, complexity, multicellular, life
Introduction
Molecular pathways responsible for cellular complexity in a given multicellular organism are those that arose and have been selected during evolution leading to that organism. By going backwards in time, or alternatively by taking contemporary representative organisms of those backward steps, ancestor cells and tissues, of every organ and organ system of the examined organism can be traced. These tissues are the result of different expression patterns, different branches of molecular pathways. Going back far enough, a eukaryotic unicellular ancestor stage can be reached. By recording the relationships (lineage) and cellularity of these stages a biological network (Albert, 2005) representing the evolutionary development of multicellular organisms could be drawn. In this fractal network a node represents a cell belonging to a given tissue in the examined organism, the tissue being the virtual descendent of a single cell in an earlier organism, and the cell being the precursor of a tissue developing in an organism to appear later (Figure 1A). Expansion of a given cell type generates new nodes connected to the same hub, which represents a progenitor cell. Differentiation generates new hubs.

The structure of such a fractal network can be described by rate of change of connectivity (node degree, k) and the rate of change of node number (N) while moving along the temporal dimension, represented by \( l_B \), the linear box size (Song et al., 2007; Song et al., 2006). Zooming in means decreasing \( l_B \), looking at pathways responsible for more and more specific cell types. Zooming out, called renormalization, means drawing simpler, more general, shared molecular networks, until reaching homeostatic networks shared by all cells in the multicellular organism that are present in the common ancestor. The number of hubs at various levels of development in an organism corresponds to cellular complexity, that is levels of organization as cells, tissues, organs, and organ systems.

Methods
The properties of such a network can be estimated by using cellular complexity expressed as the number of different cells in an organism and total cell number (N) in an organism. The dataset compiled by Bell and Mooers (Bell, 1997) was supplemented with vertebrate data compiled by Schad et al. (Schad et al., 2011) to increase the representation of complex animals, estimating the cellularity of chordates based on average weight (see Supplementary file for dataset). The network scaling relations are interpreted after Song et al. as follows (Song et al., 2006; Song et al., 2005).

Boxes provide a fractal dimension \( d_B \) that describes how relative box numbers are changing with scaling:

\[
N_B(l_B)/N \sim l_B^{-d_B}
\]

where \( N_B(l_B) \) is the number of boxes identified at linear box size \( l_B \) in a network with \( N \) nodes. When \( l_B \) is equal to \( N \), the box contains all the nodes and \( N_B \) equals 1. Consequently, plotting \( \log(N_B(l_B)/N) \) against \( \log(l_B) \) for a number of different networks a straight line (Figure 1B) corresponding to \( d_B = 1 \) is obtained.

Boxes have a degree exponent \( d_k \) that describes the relationship of degrees outside and inside of the boxes (backwards and forwards in time) as scaling changes:

\[
k_B(l_B)/k_{hub} \sim l_B^{-d_k}
\]

where \( k_B(l_B) \) is the degree of the most connected box and \( k_{hub} \) the degree of the most connected node inside the boxes. When \( l_B \) is equal to \( N \) then the box has no links and \( k_B(l_B) = 1 \), while \( k_{hub} \) will be what is observed as complexity. Consequently,

\[
l_B^{-d_k} \sim N^{-dk}
\]

Assuming that a single cell has a complexity of one and all the examined networks are descendants of this ancestral network the rule governing the generation of related (ideally linear descendant) networks can be identified by finding an average degree exponent \( d_k \) for these networks. Here linear regression weighted with \( 1/N \) to compensate for the underestimation of complexity in organisms with very high cell numbers (Figure 1B) was used.

Thus, the average value of \( d_k \) relative to \( d_B \) can be obtained from the equation of the linear regression. This in turn provides the degree distribution exponent gamma:

\[
\gamma = 1 + d_B/d_k
\]

using

\[
\gamma = 1 + d_B/(d_B - ds)
\]

where \( ds \) stands for the difference of slopes obtained from the regression (Figure 1C).

Results
The different relationships between fractal dimension and degree distribution exponent in three independently evolved multicellular groups should correspond to structural differences of cellular and molecular networks in these phylogenetic groups. At any value of gamma the corresponding fractal dimension is lower, in the order of brown algae, green algae and plants, and animals. Thus, the development of complexity corresponds to a decrease of difference between \( d_B \) and \( d_k \), a trend towards \( \gamma = 2 \), which would represent maximal diversification with a hub linked to non-identical nodes. At any particular value of \( \gamma \), plants show higher values of \( d_k \) in agreement with the observed fractal anatomy of plants. Indeed, increasing complexity corresponds to decreasing self similarity. Curves representing steps of growing complexity gradually deviate from that representing fractal dimension:

\[
d_k = (\gamma - 1)/(\gamma - 2)
\]

(Kim et al., 2007), corresponding to:

\[
\gamma = 1 + d_k/(d_k - 1)
\]
Figure 1. Cellular box-counting of multicellular life forms. A: Evolutionary fractal network. A molecular network represented by a single cell seeds the evolution of a novel tissue, which becomes an organ system with time. By using adjusted box sizes ($l_B = N$) we normalize fractal box dimension $d_B$ according to organism size. Complexity of the organism is then defined by $k_{hub}$, degree of the most connected node at a subsequent time point in evolution. Ellipses represent networks: organisms organized at various levels, the basic unit of organization being a cell. With the development of novel molecular pathways new types of cells appear; further steps, brought about by duplication or alternative splicing, refine these pathways leading to subtypes of cells in ever more complex organisms. B: Difference of slopes of fractal dimension and degree exponent. Complete renormalization generates a single box, which represents the organism at $l_B = N$. Here $N_B(l_B)/N$ is $1/N$ and $d_B = 1$. Dots represent individual species (see Supplementary file), color lines are weighted regression lines representing groups as indicated. Double headed arrows indicate the difference in slopes ($d_s$). Inset shows corresponding original approach described by Song et al. to define network fractality. C: Relationship between degree distribution and fractal dimension in different multicellular organisms. 95% confidence intervals of regression slope values are shown for the examined three different groups of multicellular life. Curves were generated online using fooplot.com.
(Figure 1C). The observed differences are not in agreement with observations on the metabolic network of bacteria and eukaryotes, where key parameters of network topology were found to be identical (Jeong et al., 2000). However, here we are not looking at conserved protein networks of metabolic activity, rather protein networks responsible for the multicellular organization of eukaryotes. Considering the dramatic differences in anatomy, physiology and metabolism in the examined groups the results are expectable.

Conclusions
Relatively simple anatomical and histological data of phylogenetically related organisms can be used to get insight into the fundamental network organisation of cells and molecules responsible for multicellularity. This method is a simple top-down approach for the investigation of cellular and molecular networks, which complements bottom-up approaches used by proteomics, metabolomics and genomics.

Further elaboration of the methodology based on network science (Jin et al., 2013) and systems biology along with further refinement of phylogenetic groups, cell and cell type numbers can provide more accurate estimations for selected organisms. Incorporation of data on the cell numbers in various tissues will allow the estimation of $d_{np}$ thereby the full description of fractal network properties. Finally, application of the method for ontologic data, examining the cellularity and complexity during the development of an organism can help draw the cell and molecular networks for any particular multicellular form of life.

Supplementary material

Supplementary File 1: Cellularity and complexity data. Data on the cellularity and complexity of a number of different organisms were compiled from the following two publications:


Taxonmical grouping follows what was used by Bell et al. Data on vertebrates in the first publication were replaced by more recent estimates in the second publication. Base 10 logarithm values were replaced by base 2 logarithm. Inverse values (1/complexity) of numbers describing cellular complexity were calculated in accordance with the proposed interpretation of $k_{bat}$. Cellularity of vertebrate organisms was calculated by using the average mass values shown and using conversion that assumes the mass of an average cell to be 7 nanograms $(7 \times 10^{-9} \text{g})$. References, with first author and date, are shown for Bell et al’s dataset.

Click here to access the data.

References


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This paper describes an analysis method and some results related to multicellular organization and complexity. While the study could be interesting, it is not well written. It is difficult to understand what is measured and what those measurements mean as described in the specific comments.

Specific comments:

1. In the introduction there are a few general statements that should be supported by general references.

2. The “eukaryotic unicellular ancestor” in the introduction represents a single cell, the ancestor of all eukaryotic cells. Is this the same as the Last Common Universal Ancestor, or LUCA? Maybe not. LUCA has been studied a lot and it appears as the ancestor of all cells including bacteria and archea. But is there a eukaryotic ancestor as well? Is it known that there was only one ancestor and only one transition from bacteria/archea to the eukaryotic cell? If so, is there any study that can back up such a statement?

3. Is dB on the right hand side of equation 1 supposed to be d_B (i.e., B in subscript)? Similarly, dk is likely supposed to be d subscript k in equation 2.

4. Please explain where equation 4 comes from.

5. Please explain better what the data represent. There is a statement that N is the total number of cells in an organism. What is then N_B? Is it the number of different types of cell? And what is the network itself? There is a statement that “boxes have a degree exponent d_k” (page 2, right column, first line). But what is a box? Is it a cell itself? And what is the network inside the box? Or is it that the smallest box is a single cell and inside a box can only looked at when the box represent an organ? Yet towards the end of the Result, it is stated that “rather protein networks responsible for the multicellular organization of eukaryotes”. But I do not see any analysis on protein networks. All these questions arise because the methods is unclear and incomplete.

6. If complexity here means intercellular network complexity characterized by the degree distribution, then it is obviously different than the complexity of protein networks. It is not obvious why one should expect protein network to be self-similar with cell networks.
Is the rationale for developing the new method (or application) clearly explained?
Partly

Is the description of the method technically sound?
Partly

Are sufficient details provided to allow replication of the method development and its use by others?
No

If any results are presented, are all the source data underlying the results available to ensure full reproducibility?
Yes

Are the conclusions about the method and its performance adequately supported by the findings presented in the article?
Partly

Competing Interests: No competing interests were disclosed.

Referee Expertise: Biomechanics, mechanobiology, complexity

I have read this submission. I believe that I have an appropriate level of expertise to confirm that it is of an acceptable scientific standard, however I have significant reservations, as outlined above.

George W. Bassel
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The authors present a method to measure cellular complexity in different species by examining fractal network properties. This is potentially a very interesting method, yet there are several things which should be addressed:

1. As this is a methods paper, it would be nice to see how this particular method of measuring cellular complexity relates to others. There is no benchmark presented for the comparison of results.

2. It may not immediately be obvious to readers how fractals relate to complexity of an organism. The method illustrated in Fig. 1A could be more clear for readers who are not familiar with fractals, showing an example of how box-counting is actually carried out, and how this relates to complexity.

3. The results presented in Fig. 1 could be discussed in greater detail. It is not clear why there is a fairly noisy relationship between fractal dimension and degree exponent between species within different evolutionary backgrounds. Could this variance be due to the data that were used?
4. Though it is possible to measure cellular complexity with this approach, it is not clear why this method is of particular value, and what purposes it would serve aside from the example presented. The addition of more relevant context in the introduction and conclusions could help with this.

Is the rationale for developing the new method (or application) clearly explained?
Partly

Is the description of the method technically sound?
Partly

Are sufficient details provided to allow replication of the method development and its use by others?
Yes

If any results are presented, are all the source data underlying the results available to ensure full reproducibility?
Yes

Are the conclusions about the method and its performance adequately supported by the findings presented in the article?
Partly

**Competing Interests:** No competing interests were disclosed.

I have read this submission. I believe that I have an appropriate level of expertise to confirm that it is of an acceptable scientific standard, however I have significant reservations, as outlined above.

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