Rampant software errors may undermine scientific results

[version 2; peer review: 2 approved]

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Abstract
The opportunities for both subtle and profound errors in software and data management are boundless, yet they remain surprisingly underappreciated. Here I estimate that any reported scientific result could very well be wrong if data have passed through a computer, and that these errors may remain largely undetected. It is therefore necessary to greatly expand our efforts to validate scientific software and computed results.

Keywords
data management, software error

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Computational results are particularly prone to misplaced trust

Perhaps because of ingrained cultural beliefs about the infallibility of computation\(^1\), people show a level of trust in computed outputs that is completely at odds with the reality that nearly zero provably error-free computer programs have ever been written\(^2,3\).

It has been estimated that the industry average rate of programming errors is “about 15 – 50 errors per 1000 lines of delivered code”\(^4\). That estimate describes the work of professional software engineers—not of the graduate students who write most scientific data analysis programs, usually without the benefit of training in software engineering and testing\(^5,6\). The recent increase in attention to such training is a welcome and essential development\(^7–11\).

Nonetheless, even the most careful software engineering practices in industry rarely achieve an error rate better than 1 per 1000 lines. Since software programs commonly have many thousands of lines of code (\textit{Table 1}), it follows that many defects remain in delivered code—even after all testing and debugging is complete.

Software errors and error-prone designs are compounded across levels of design abstraction. Defects occur not only in the top-level program being run but also in compilers, system libraries, and even firmware and hardware—and errors in such underlying components are extremely difficult to detect\(^12\).

How frequently are published results wrong due to software bugs?

Of course, not every error in a program will affect the outcome of a specific analysis. For a simple single-purpose program, it is entirely possible that every line executes on every run. In general, however, the code path taken for a given run of a program executes only a subset of the lines in it, because there may be command-line options that enable or disable certain features, blocks of code that execute conditionally depending on the input data, etc. Furthermore, even if an erroneous line executes, it may not in fact manifest the error (i.e., it may give the correct output for some inputs but not others). Finally: many errors may cause a program to simply crash or to report an obviously implausible result, but we are really only concerned with errors that propagate downstream and are reported.

In combination, then, we can estimate the number of errors that actually affect the result of a single run of a program, as follows:

\[
\text{Number of errors per program execution} = \frac{\text{total lines of code (LOC)}}{\text{proportion executed}} \times \frac{\text{probability of error per line}}{\left(\text{probability that the error meaningfully affects the result}\right)} \times \left(\text{probability that an erroneous result appears plausible to the scientist}\right)
\]

For these purposes, using a formula to compute a value in Excel counts as a “line of code”, and a spreadsheet as a whole counts as a “program”—so many scientists who may not consider themselves coders may still suffer from bugs\(^13\).

All of these values may vary widely depending on the field and the source of the software. Consider the following two scenarios, in which the values are nothing more than educated guesses (informed, at least, by deep experience in software engineering).

\begin{table}[h]
\centering
\caption{Number of lines of code in typical classes of computer programs (via informationisbeautiful.net).}
\begin{tabular}{|l|l|}
\hline
\textbf{Software Type} & \textbf{Lines of Code} \\
\hline
Research code supporting a typical bioinformatics study, e.g. one graduate student-year. & \(O(1000) – O(10,000)\) \\
Core scientific software (e.g. Matlab and R, not including add-on libraries). & \(O(100,000)\) \\
Large scientific collaborations (e.g. LHC, Hubble, climate models). & \(O(1,000,000)\) \\
Major software infrastructure (e.g. the Linux kernel, MS Office, etc.). & \(O(10,000,000)\) \\
\hline
\end{tabular}
\end{table}
Scenario 1: A typical medium-scale bioinformatics analysis

- 100,000 total LOC (neglecting trusted components such as the Linux kernel).
- 20% executed
- 10 errors per 1000 lines
- 10% chance that a given error meaningfully changes the outcome
- 10% chance that a consequent erroneous result is plausible

Multiplying these, we expect that two errors changed the output of this program run, so the probability of a wrong output is effectively 100%. All bets are off regarding scientific conclusions drawn from such an analysis.

Scenario 2: A small focused analysis, rigorously executed

Let’s imagine a more optimistic scenario, in which we write a simple, short program, and we go to great lengths to test and debug it. In such a case, any output that is produced is in fact more likely to be plausible, because bugs producing implausible outputs are more likely to have been eliminated in testing.

- 1000 total LOC
- 100% executed
- 1 error per 1000 lines
- 10% chance that a given error meaningfully changes the outcome
- 50% chance that a consequent erroneous result is plausible

Here the probability of a wrong output is 5%.

The factors going into the above estimates are rank speculation, and the conclusion varies widely depending on the guessed values. Measuring such values rigorously in different contexts would be valuable but also tremendously difficult. Nonetheless it is sobering that some plausible values can produce high total error rates, and that even conservative values suggest that an appreciable proportion of results may be erroneous due to software defects—above and beyond those that are erroneous for more widely appreciated reasons.

Put another way: publishing a computed result amounts to asserting that the likelihood of error is acceptably low, and thus that the various factors contributing to the total error rate are low. In the context of a specific program, the first three factors (# LOC, % executed, and errors/line) can be measured or estimated. However the last two (“meaningful change” and “plausible change”) remain completely unknown in most cases. In the following two sections I argue that these two factors are likely large enough to have a real impact. It is therefore incumbent on scientists to validate computational procedures—just as they already validate laboratory reagents, devices, and procedures—in order to convince readers of the absence of serious bugs.

Software is exceptionally brittle

A response to concerns about software quality that I have heard frequently—particularly from wet-lab biologists—is that errors may occur but have little impact on the outcome. This may be because only a few data points are affected, or because values are altered by a small amount (so the error is “in the noise”). The above estimates account for this by including a term for “meaningful changes to the result”. Nonetheless, in the context of physical experiments, it is tempting to believe that small errors tend to reduce precision but have less effect on accuracy—i.e. if the concentration of some reagent is a bit off then the results will also be just a bit off, but not completely unrelated to the correct result.

But software is different. We cannot apply our physical intuitions, because software is profoundly brittle: “small” bugs commonly have unbounded error propagation. A sign error, a missing semicolon, an off-by-one error in matching up two columns of data, etc. will render the results complete noise. It is rare that a software bug would alter a small proportion of the data by a small amount. More likely, it systematically alters every data point, or occurs in some downstream aggregate step with effectively global consequences. In general, software errors produce outcomes that are inaccurate, not merely imprecise.

Many erroneous results are plausible

Bugs that produce program crashes or completely implausible results are more likely to be discovered during development, before a program becomes “delivered code” (the state of code on which the above errors-per-line estimates are based). Consequently, published scientific code often has the property that nearly every possible output is plausible. When the code is a black box, situations such as these may easily produce outputs that are simply accepted at face value:

- An indexing off-by-one error or other data management mistake associates the wrong pairs of X’s and Y’s.
- A correlation is found between two variables where in fact none exists, or vice versa.
- A sequence aligner reports the “best” match to a sequence in a genome, but actually provides a lower-scoring match.
- A protein structure produced from x-ray crystallography is wrong, but it still looks like a protein.
- A classifier reports that only 60% of the data points are classifiable, when in fact 90% of the points should have been classified (and worse, there is a bias in which points were classified, so those 60% are not representative).
- All measured values are multiplied by a constant factor, but remain within a reasonable range.

Software errors and statistical significance are orthogonal issues

A software error may produce a spurious result that appears significant, or may mask a significant result.
If the error occurs early in an analysis pipeline, then it may be considered a form of measurement error (i.e., if it systematically or randomly alters the values of individual measurements), and so may be taken into account by common statistical methods.

However: typically the computed portion of a study comes after data collection, so its contribution to wrongness may easily be independent of sample size, replication of earlier steps, and other techniques for improving significance. For instance, a software error may occur near the end of the pipeline, e.g. in the computation of a significance value or of other statistics, or in the preparation of summary tables and plots.

The diversity of the types and magnitudes of errors that may occur makes it difficult to make a general statement about the effects of such errors on apparent significance. However it seems clear that, a substantial proportion of the time (based on the above scenarios, anywhere from 5% to 100%), a result is simply wrong—rendering moot any claims about its significance.

**Popular software is not necessarily less bug-prone**

The dangers posed by bugs should be obvious to anyone working with niche or custom software, such as one-off scripts written by a graduate student for a specific project. Still it is tempting to think that “standard” software is less subject to these concerns: if everyone in a given scientific field uses a certain package and has done so for years, then surely it must be trustworthy by now, right? Sadly this is not the case.

In the open-source software community this view is known as “Linus’s Law”: “Given enough eyeballs, all bugs are shallow”. The law may in fact hold when there are really many eyeballs reading and testing the code. However widespread usage of the code does not produce the same effect. This has been recently demonstrated by the discovery of major security flaws in two extremely widely used open-source programs: the “Shellshock” bug in the bash command line shell and the “Heartbleed” bug in the OpenSSL encryption library. In both cases, code that runs on a substantial fraction of the world’s computers is maintained by a very small number of developers. Despite the code being open-source, “Linus’s Law” did not take effect simply because not enough people read it—even over the course of 25 years, in the case of Shellshock.

This principle applies not only to the software itself, but also to computed results that are reused as static artifacts. For instance, it took 15 years for anyone to notice errors in the ubiquitous BLOSUM62 amino acid substitution matrix used for protein sequence alignment.

Furthermore, even popular software is updated over time, and is run in different environments that may affect its behavior. Consequently, even if a specific version of a package running on a specific computer is considered reliable, that trust cannot necessarily be extended to other versions of the same software, or to the software when run on a different CPU or on a different operating system.

**What can be done?**

All hope is not lost; we must simply take the opportunity to use technology to bring about a new era of collaborative, reproducible science. Open availability of all data and source code used to produce scientific results is an incontestable foundation. A culture of comprehensive code review (both within and between labs) can certainly help reduce the error rate, but is not a panacea. Beyond that, we must redouble our commitment to replicating and reproducing results, and in particular we must insist that a result can be trusted only when it has been observed on multiple occasions using completely different software packages and methods.

A flexible and open system for describing and sharing computational workflows would allow researchers to more easily examine the provenance of computational results, and to determine whether results are robust to swapping purportedly equivalent implementations of computational steps. A shared workflow system may thereby facilitate distributed verification of individual software components. Projects such as Galaxy, Kepler, and Taverna have made inroads towards this goal, but much more work is needed to provide widespread access to comprehensive provenance of computational results. Perhaps ironically, a shared workflow system must itself qualify as a “trusted component”—like the Linux kernel—in order to provide a neutral platform for comparisons, and so must be held to the very highest standards of software quality. Crucially, any shared workflow system must be widely used to be effective, and gaining adoption is more a sociological and economic problem than a technical one. The first step is for all scientists to recognize the urgent need to verify computational results—a goal which goes hand in hand with open availability of comprehensive provenance via workflow systems, and with verification of the individual components of those workflows.

**Competing interests**

No competing interests were disclosed.

**Grant information**

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C. Titus Brown
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This is a sober (and sobering) perspective on the likely frequency of software errors, and the author has addressed all of my concerns in the revision.

Competing Interests: No competing interests were disclosed.

I confirm that I have read this submission and believe that I have an appropriate level of expertise to confirm that it is of an acceptable scientific standard.

Reviewer Report 04 August 2015

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Daniel S. Katz
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This version of the paper is much improved, and in general, I agree with the author's response comments. I still have some concerns with two issues, and reading the paper made me think of one more point of interest, but in general, I am satisfied to see this paper move forward as accepted.

The first issue I have is in the description of the scenarios, where the first says that in a somewhat typical analysis, the probability of a wrong output is 100%. This says to me that there is something wrong with the calculations, as I don't think typical outputs are 100% likely to be incorrect.
My second issue is the discussion of workflows in the final paragraph. While there are indeed a set of computations that are described as workflows, particularly data analysis applications, there is also a large set that are not workflows, particularly simulation applications, that are much better described as monolithic programs (though using subroutines, methods, objects, etc. internally). I don't think the workflow discussion is needed in this paper, or that it really helps make the key points.

Finally, as an additional point, it would be interesting to compare this paper with work done in fault tolerance (aka resilience) where errors in hardware lead to different types of errors in the application, ranging from hangs and crashes to detectable errors to insignificant or significant undetectable errors. From my own work, http://www.slideshare.net/danielskatz/aft-dsk-reefinalreviewmay2001 provides an example of this, though there are likely many peer-reviewed published works that could also be used for a source of a comparison.

**Competing Interests:** No competing interests were disclosed.

I confirm that I have read this submission and believe that I have an appropriate level of expertise to confirm that it is of an acceptable scientific standard.
This is not easy, but it would be worthwhile, similar to the author’s statement, “Measuring such values rigorously in different contexts would be valuable but also tremendously difficult” (but at a different level). If “most scientific results are probably wrong,” the author should be able to select a relatively small number of papers and demonstrate how software errors led to wrong results. I would like to see such an experiment, which would serve to verify this paper, rather than it standing as an unverified claim about verification.

Finally, there is the classic problem with verification of a model (software, in this case): that fact that it works well in one domain is no guarantee that it will work well in another domain.

Having made these objections to the degree of the illness of the patient, I mostly agree with remedies discussed in the last section. Open available of data and code is clearly good for both trust and reproducibility. Running (computational) experiments multiple ways can help find any errors in any one of them, assuming they do not use common components (e.g., libraries, tools, or even hardware) that could lead to systematic biases. But how this should be done is less clear. For example, we have enough workflow systems that I don’t see any need for any one of them to be more trusted than the code that runs on them; we can just use different workflow systems with different code as part of the testing.

Back to the author’s last point, I agree that “to recognize the urgent need” is essential, but to me, the need is verification; I could read this closing comment as saying that the need is widely adopted and widely trusted workflow tools. This should be clarified.

In summary, this paper could be better titled and less strongly worded in places, and the paper itself needs to be verified. An alternate title would be one that makes the point, “Software, like other experiments, must be verified to be trusted”

**Competing Interests:** No competing interests were disclosed.

I confirm that I have read this submission and believe that I have an appropriate level of expertise to confirm that it is of an acceptable scientific standard, however I have significant reservations, as outlined above.

Author Response 20 Jul 2015

David Soergel,

Thanks very much for your insightful comments, and apologies for the long-delayed response. I believe I have addressed the main point about softening the claims throughout the paper. Some further thoughts follow:

“First, I think this statement is overly focused on software. One method for developing trust in results from a particular code is that they match results from other codes. Another method is that they match results from experiment. A third method might be based on code review."

I focus on software because I think it is commonly trusted far out of proportion with its level of validation. Everyone understands that physical measurements must be validated, devices must be calibrated, experiments should ideally be reproduced in other labs, etc.-- but code seems to be a cultural blind spot in this regard.

When a computational result can be directly compared to an experimental result, then of course
agreement should increase trust in both. More commonly, I think, a given result arises from a combination of experiment ("data collection") and computation ("data analysis"), and comparisons can only be made between attempts incorporating both. Again agreement from multiple attempts should increase trust--but only if the analysis steps lack common components. This is another reason to focus on software: software is typically used downstream of data collection, so a bug can easily mask whatever signal is present in the underlying data, producing spurious agreement or spurious disagreement in the final result. Because software often has the last word in generating a result, then, it demands an even higher level of trust than upstream inputs.

Code review is certainly a good thing, but in my view is never sufficient to generate trust. Anecdotally, I've found plenty of bugs in code that was already reviewed. In any case, "code review" means many things to many people, and obviously the likelihood of finding bugs varies widely with the skill of the reviewer.

"Second, this statement is not only true for software, it is also true for this complete paper. In order to believe the chances for errors claimed here, this paper itself needs to be verified, and not at the level of each assumption made internally (in the "How frequently ..." section), but at the level of the overall claim. This is not easy, but it would be worthwhile, similar to the author's statement, "Measuring such values rigorously in different contexts would be valuable but also tremendously difficult" (but at a different level). If "most scientific results are probably wrong," the author should be able to select a relatively small number of papers and demonstrate how software errors led to wrong results. I would like to see such an experiment, which would serve to verify this paper, rather than it standing as an unverified claim about verification."

This is an opinion piece; I hope the more speculative language now makes clear that I am expressing justifiable anxiety that a serious problem may exist, rather than asserting that it definitely does exist. I certainly agree that verifying my estimates would be a great thing to do (particularly the aggregate error rate, not just the individual factors, as you point out). However I think that would be a major undertaking that is not tractable for me to do in this paper.

I do already cite a number of cases where software bugs resulted in wrong results, but these are basically anecdotal, and of course they are the ones that have already been found and reported. The proportion of these to the overall literature is vanishingly small. There are surely many more papers where an author or reader is privately aware of an error. And a still much larger proportion of papers, I believe (but cannot prove), contain errors that remain completely unknown.

I can think of only two ways to determine that proportion empirically. The first is to identify existing attempts to reproduce results, confirm that they are not subject to common sources of error, and track down the causes of any disagreement. This method may be subject to selection bias (i.e. in general, only important or controversial results get replication attempts in the first place).

The second is to take a random sample of papers and attempt to fully reproduce them, or at least to carefully review the code in search of errors. That would be really a lot of work-- in one example, an independent reproduction of a single computational study took 3 months. A systematic campaign to reproduce computational results would be great, inspired by similar efforts focusing on reproducing experimental results (e.g. the Amgen study and the OSF Reproducibility Project).

But I can't take it on alone! Rather I hope this paper helps to demonstrate the need for researchers, funders, and publishers to take code verification more seriously, and to foster the
reproduction studies that would be needed to confirm or deny my estimates. Crucially, it's not just a matter of successfully running a study author's code (which, in the example case of in ACM conferences and journals, can be downloaded and compiled for only about half of the papers anyway). Journal policies requiring at least that level of replication would be a good start. But really the point here is to use different code to generate the same result.

So I think we agree: I am making an unverified claim about verification, and I too would like to see it verified.

“Finally, there is the classic problem with verification of a model (software, in this case): that fact that it works well in one domain is no guarantee that it will work well in another domain.”

True, we can never make absolute guarantees. But we can do better than the status quo, which all too often provides no verification at all. Also, this point opens the question of the breadth of applicability of a given software artifact: some software does only a very specific thing, and so can be thoroughly verified within its single domain, while other software is very generic and so is much harder to verify across domains. I don't address this in the paper, except to the extent that the factor for "proportion of lines executed" is tangentially related (e.g., successful tests exercising some code paths say nothing about runs taking different code paths). That factor could be thought of more abstractly as the likelihood that verification in one domain should generate trust in another.

“Having made these objections to the degree of the illness of the patient, I mostly agree with remedies discussed in the last section. Open available of data and code is clearly good for both trust and reproducibility. Running (computational) experiments multiple ways can help finds any errors in any one of them, assuming they do not use common components (e.g., libraries, tools, or even hardware) that could lead to systematic biases. But how this should be done is less clear. For example, we have enough workflow systems that I don't see any need for any one of them to be more trusted than the code that runs on them; we can just use different workflow systems with different code as part of the testing."

I agree that the ideal way to gain trust in a particular result is to observe agreement from two experiments in which *everything* differs, even the workflow system and the hardware (at some length: http://davidsoergel.com/posts/confirmation-depth-as-a-measure-of-reproducible-scientific-research, but just see Fig. 2 there for the main point).

However: if we could agree on a common, trusted workflow system, that would make it much easier both to verify software components and to track down sources of error, simply by swapping out individual components of workflows with purportedly equivalent alternative implementations. When components are reused across workflows (and across labs, etc.), crowdsourced results from such component-swap experiments would quickly reveal which components are most commonly associated with robust results. I'll have to describe that vision more thoroughly elsewhere, but for now I hope it points at one thing I hope we could gain from standardizing workflow and provenance descriptions. Perhaps more simply: researchers are more likely to examine (and perhaps tweak and reuse) a workflow written in a language (or graphical notation, etc.) with which they are already familiar; Balkanization of workflow systems largely defeats their purpose.

“Back to the author’s last point, I agree that "to recognize the urgent need is essential, but to me,
I did really mean both things--I've tried to clarify that.

Thanks again for the very helpful comments!

**Competing Interests:** No competing interests were disclosed.
It might be worth adding a reference to the recent SSH debacle, where it turned out that incredibly well used software had a significant flaw. In other words, it's not enough for software to be well used for it to be correct! (Space permitting.)

**Competing Interests:** No competing interests were disclosed.

I confirm that I have read this submission and believe that I have an appropriate level of expertise to confirm that it is of an acceptable scientific standard, however I have significant reservations, as outlined above.

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**Author Response 18 Dec 2014**

**David Soergel,**

Thanks for the kind and helpful comments! The editors prefer to wait for more reviews before issuing a revision, but in the meantime:

1. In the title, I could go with "...may undermine...". (The loss in pithiness is indeed a shame, but so be it).

2. Agreed re rearranging and toning down the abstract.

3. I'll do another search for references and justifications for the ballpark estimates of % LOC executed and so on, but I expect this one will be hard because there's so much variation. For now the numbers are just my intuitions based on experience; I can try to clarify that at least. I think the fuzziest one is the plausibility term-- I know of no effort to measure that, and am not even sure how you'd go about it. In the course of code development and data analysis, how often do you look at a result and think "that's just not right"? That one varies too with the paranoia level of the scientist. (e.g., I'm a big fan of doing sanity checks that may reveal that some result is not plausible, even if that fact was not immediately obvious).

Thanks for the citation suggestions. They're both already in there, actually (15 and 3, respectively), but I'll cite them from additional places as you suggest.

And yes, I'll add a para mentioning "Linus's Law" ("Given enough eyeballs, all bugs are shallow") and the recent counterexamples (Heartbleed, Goto Fail, and Shellshock). These are notable because they're all security vulnerabilities, which (perhaps rightly) get a lot more press than bugs of other kinds. There's also a world of difference between widespread "usage" and widespread "reading the code"-- a distinction that is sometimes glossed over in these discussions.

Thanks again for the comments!

**Competing Interests:** No competing interests were disclosed.

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**Author Response 20 Jul 2015**

**David Soergel,**

Thanks again for the comments, and apologies for the long-delayed response. The changes described above are reflected in the new version.
I have some data on software error (fault) rates at my website, panko.com, under the human error branch. In unit testing, which occurs when a module has been coded and desk-checked developer, the error rate is 10 to 50 errors per thousand lines of code (KLOC), with an average of about 30 to 40. However, in commercial software development, extensive testing reduces this to about 1 to 3 errors per KLOC at the end of system development. However, commercial software firms spend about a third to half as much on testing as they do on coding. I'm guessing that few purpose-built studies do anything like that level of testing, so I would expect errors somewhere in between. As a caveat, software studies report defects, which are either quantitative or qualitative errors. Only quantitative errors will affect results. Qualitative errors are poor programming practices that may lead to a quantitative error later or may not. I have not data on the likelihood on the percentage of errors large enough to affect results, but about a quarter of all reported faults are serious in most code inspections that have measured them. Turning to spreadsheets, I have data on spreadsheet audits on the spreadsheet research branch of my website. Of 55 operational spreadsheet inspections that only reported errors that were serious in context (could cause the wrong decision, a material value in accounting, etc.), 91% had at least one error. The quality of these inspections was generally much more cursory than software code inspection. More broadly, in software development, one never expects to have completely error-free programs of even moderate size. This is true of any human work product. We should be asking how science should deal with the actual certainty of error in scientific software. That is not being alarmist. It is a serious question given the realities of human error and scientific evidence about these errors. Thank you for doing this study.

Ray Panko, University of Hawaii, ray@panko.com

Competing Interests: I have no competing interests.
Scientific Python ecosystem. In one case the other implementation was written in Matlab, in the other Mathematica was used. Each of these implementations was written by a person with significant experience with his/her chosen platform.

For each problem, both authors tested their implementation until they considered it good for use in published work. Upon comparison, small differences were found and tracked down - fortunately they weren't just due to uncontrollable differences in floating-point computations. In both cases, both implementations turned out to have minor bugs. However, when the results ultimately agreed and more tests had been done, the final "official" results were not very different from what the original implementations had produced. The bugs were of the kind described in this article: an average computed over a data series minus the last point (off-by-one error), a wrong criterion in a data filter, a typo in a numerica constant, etc.

I think it would be interesting to do such studies on a much larger scale, and see if the article's estimates turn out to be reasonable.

**Competing Interests:** No competing interests were disclosed.