SUPPLEMENTARY TEXT 1

Dynamics of the lateral inhibition model under synchronous and asynchronous updates

The 2 cell model as displayed in panel (A) below is a simple positive regulatory circuit with 4 regulatory components (two Green and 2 Red), 2 activations (denoted by normal arrows) and 2 inhibitions (denoted by blunt arrows). The behaviour of such an elementary circuit has been fully characterised by Remy et al. [1]. The synchronous and asynchronous State Transition Graphs of this model are shown below. The two stable states are coloured depending on which Green and Red components are active in cells 1 and 2 (same colour code as in Fig. 1, main text). Starting from a "naive" state where all the components are set to 0, the synchronous dynamics is trapped in a terminal cycle (panel (B)), whereas the asynchronous dynamics ends up in one of the two stable states (panel (C)). When considered over a 2D grid of cells, these behaviours are reproduced, leading to oscillations under a synchronous update (Fig. 1-B, main text) or to a stable pattern when cells are updated asynchronously enough (Fig. 1, panels C-F, main text).

![State Transition Graphs](image)